

### Solubility #1

1. Write the net ionic equation(s) for the reaction(s) when equal volumes of 0.2 M  $\text{Sr}(\text{OH})_2$  and 0.2 M  $\text{Fe}_2(\text{SO}_4)_3$  are mixed.
2. Describe the equilibrium that exists in a saturated solution of  $\text{BaSO}_4$  in contact with some solid residue of  $\text{BaSO}_4$ .
3. In an experiment, 0.1 M  $\text{AgNO}_3$  is added to 0.1 M  $\text{NaCl}$ , resulting in the formation of a white precipitate. When 0.1 M  $\text{NaI}$  is added to this mixture, the white precipitate dissolves and a yellow precipitate forms.
  - (a) Write the formula and name for each of the following:
    - (i) the white precipitate
    - (ii) the yellow precipitate
  - (b) Write the net ionic equation to represent the formation of the more soluble precipitate.
4. A solution of  $\text{Ba}(\text{NO}_3)_2$  is added to a solution of  $\text{Na}_2\text{CO}_3$ , resulting in the formation of a white precipitate that reacts with  $\text{HNO}_3$ .
  - (a) Write a net ionic equation to represent the formation of the white precipitate.
  - (b) Explain why the precipitate reacts in  $\text{HNO}_3$ .
5. A student is given three beakers, each containing 100 mL of solution. The first beaker contains 0.20 M  $\text{CaS}$ ; the second contains 0.20 M  $\text{CuSO}_4$ ; the third contains 0.20 M  $\text{Sr}(\text{OH})_2$ . The student is asked to select two solutions which, when combined, would result in the formation of a mixture containing a single precipitate.
  - (a) Which two solutions should the student use?
  - (b) Write the net ionic equation for the precipitation reaction.
6. If a solution of calcium nitrate is added to a saturated solution of calcium sulphate, a precipitate is observed to form. Explain why this occurs, including any relevant equation(s) and identify the precipitate.

7. Write an equation that describes a saturated solution of NaCl.
8. A solution containing  $\text{Al}^{3+}$ ,  $\text{NH}_4^+$  and  $\text{Mg}^{2+}$  ions is added to a solution containing  $\text{S}^{2-}$ ,  $\text{Cl}^-$  and  $\text{OH}^-$  ions. Identify the ions that do not form a precipitate.
9. Write an equation that describes the equilibrium present in a saturated solution of  $\text{Cu}_3(\text{PO}_4)_2$ .
10. A 1.0 M solution of sodium sulphide is added to a 1.0 M solution of copper(II) chloride resulting in the formation of a precipitate.
- (a) Identify the precipitate.
  - (b) Write the complete ionic equation for the reaction.
  - (c) Identify all spectator ions.
11. Identify a salt that could be added to a saturated solution of  $\text{BaSO}_4$  that would result in more solid barium sulphate forming.
12. Write an equation that describes a saturated solution of magnesium hydroxide.
13. When solid  $\text{Ca}(\text{NO}_3)_2$  is added to a saturated solution of  $\text{MgCO}_3$ , more  $\text{MgCO}_3$  dissolves. Explain.
14. A student mixes equal volumes of 0.20 M  $\text{Na}_2\text{CO}_3$  and 0.20 M  $\text{Ba}(\text{NO}_3)_2$ , forming a white precipitate.
- (a) Write the net ionic equation for the precipitation reaction.
  - (b) Explain why the precipitate dissolves when HCl is added.
15. Write an equation that represents the solubility equilibrium of a saturated solution of barium sulphate.

## Solubility #2

1. A solution contains  $\text{SO}_4^{2-}$  and  $\text{Cl}^-$ . Outline an experimental procedure to remove each ion individually from the solution, and identify the reagents used in the procedure.
2. A solution is known to contain  $\text{Cu}^+$ ,  $\text{Be}^{2+}$  and  $\text{Sr}^{2+}$  ions, each at a concentration of 0.20 M.
  - (a) What compound could be used to precipitate the  $\text{Sr}^{2+}$  while leaving the other two cations in solution?
  - (b) Write the net ionic equation for the reaction
3. A solution contains  $\text{Pb}^{2+}$ ,  $\text{Mg}^{2+}$ , and  $\text{Sr}^{2+}$ . Outline a procedure to isolate the precipitate  $\text{SrSO}_4$  from this solution.
4. Write the formula of two materials (other than water) that could be added to a saturated solution of  $\text{Ag}_2\text{CO}_3$  to increase the amount of  $\text{Ag}_2\text{CO}_3$  that will dissolve.
5. A solution contains  $\text{Ca}^{2+}$ ,  $\text{Sr}^{2+}$  and  $\text{Pb}^{2+}$  ions that must be separated.
  - (a) Identify an anion that could be used to remove only the lead ion by precipitation.
  - (b) Identify an anion that could be used to separate  $\text{Ca}^{2+}$  from  $\text{Sr}^{2+}$ .

6. Use the table of solubilities to determine a scheme that allows the separation of  $\text{Ba}^{2+}$ ,  $\text{Cu}^{2+}$ , and  $\text{Br}^-$  from each other.
7. Use the table of solubilities to describe how you would separate  $\text{Mg}^{2+}$ ,  $\text{Ba}^{2+}$  and  $\text{Ag}^+$  from each other.
8. Use the table of solubilities to outline a scheme to separate a mixture of  $\text{Li}^+$ ,  $\text{Ag}^+$ ,  $\text{Sr}^{2+}$  and  $\text{Fe}^{3+}$  from each other.
9. A beaker contains  $\text{OH}^-$  ions and  $\text{S}^{2-}$  ions in solution both at a concentration of 0.10 M. You are asked to precipitate the  $\text{OH}^-$  ions while leaving the  $\text{S}^{2-}$  ions in solution.
- (a) Which reagent could you use?
- (b) Write the net ionic equation for the precipitation reaction.

Solubility #3 - Assume that all solutions are at 25°C unless told otherwise.

1. Which one of the following solutions will contain the greatest silver ion concentration?  
saturated  $\text{Ag}_2\text{CO}_3$                       saturated  $\text{AgCl}$
2. In which solution would you find the highest magnesium ion concentration: saturated  $\text{MgCO}_3$  or saturated  $\text{Mg}(\text{OH})_2$ ?
3. The  $K_{sp}$  values for various silver salts are given below:

$\text{AgBrO}_3$	$5.3 \times 10^{-5}$	$\text{Ag}_2\text{CO}_3$	$8.5 \times 10^{-12}$
$\text{Ag}_2\text{Cr}_2\text{O}_7$	$2.0 \times 10^{-7}$	$\text{AgSCN}$	$1.2 \times 10^{-12}$
$\text{AgOH}$	$1.5 \times 10^{-10}$	$\text{AgBr}$	$5.4 \times 10^{-13}$
$\text{AgCl}$	$1.8 \times 10^{-10}$	$\text{AgI}$	$8.5 \times 10^{-17}$
$\text{Ag}_2\text{CrO}_4$	$1.1 \times 10^{-12}$	$\text{AgIO}_3$	$3.2 \times 10^{-8}$

Determine which one of these compounds gives the highest silver ion concentration in a saturated solution and calculate this concentration.

4. Calculate the solubility of  $\text{BaSO}_4$ .
5. Calculate the mass of solid  $\text{PbSO}_4$  that can be dissolved in 5.0 L of solution at 25°C.
6. Calculate the solubility of  $\text{PbI}_2$  at 25°C.
7. What is the solubility of calcium oxalate at 25°C in g/L?
8. How many milligrams of  $\text{CaCO}_3$  would be dissolved in 1.0 L of saturated solution at 25°C.
9. What mass of  $\text{PbI}_2$  will dissolve in 250 mL of water?
10. a. What is the solubility of magnesium hydroxide?  
b. What is the  $[\text{OH}^-]$  in a saturated solution of magnesium hydroxide?

#### Solubility #4

1. When excess  $\text{Ag}_2\text{CO}_3$  solid is shaken with 1.00 L of 2.00 M  $\text{K}_2\text{CO}_3$ , it is determined that  $6.00 \times 10^{-6}$  mol  $\text{Ag}_2\text{CO}_3$  solid dissolves. Calculate the solubility product for silver carbonate.
2. Calculate the  $K_{sp}$  for  $\text{SrF}_2$  if the solubility is 0.122 g/L.
3. A saturated solution of calcium hydroxide is found to have  $[\text{OH}^-]$  of  $2.09 \times 10^{-2}$  M. Calculate the  $K_{sp}$  for  $\text{Ca}(\text{OH})_2$ .
4. The solubility of  $\text{Ag}_2\text{SO}_4$  is 0.62 g/L at  $6^\circ \text{C}$ . What is the  $K_{sp}$  at this temperature?
5. Describe an analytical method which could be used to determine the  $K_{sp}$  of a saturated solution of silver sulphate other than drying the solid from a saturated solution.
6. At  $20^\circ \text{C}$  the solubility of  $\text{PbF}_2$  is 64 mg per 100 mL of solution. Determine the  $K_{sp}$  for lead II fluoride.
7. The equilibrium in a saturated  $\text{ZnI}_2$  solution is given by:



Predict the effect on the solubility of  $\text{ZnI}_2$  of adding some:

- (a) solid  $\text{NaI}$ .
- (b) solid  $\text{Zn}(\text{NO}_3)_2$
- (c) solid  $\text{NaOH}$
- (d) concentrated  $\text{HCl}$
- (e) solid  $\text{NH}_4\text{NO}_3$

### Solubility #5

1. What is the minimum mass of  $\text{Na}_2\text{SO}_4$  crystal that must be dissolved in 5.0 L of 0.0010 M  $\text{Ca}(\text{NO}_3)_2$  solution in order to initiate precipitation of calcium sulphate?
2. 750 mL of a  $1.0 \times 10^{-2}$  M lead II chloride solution was cooled resulting in the precipitation of 1.80 g of solid  $\text{PbCl}_2$ . What is the molarity of the cooled solution?
3. Determine the mass of silver chloride precipitated when 50 mL of 0.60 M  $\text{AgNO}_3$  solution is mixed with 100 mL of 0.10 M  $\text{CaCl}_2$  solution. Assume  $\text{AgCl}$  has negligible solubility.
4. A given sample of water with temporary hardness has a  $[\text{Ca}^{2+}]$  of  $1.0 \times 10^{-3}$  M.  
(a) If the  $K_{\text{sp}}$  of  $\text{CaF}_2$  is  $1.7 \times 10^{-10}$ , what is the maximum  $[\text{F}^-]$  that can be attained in temporary hard water before  $\text{CaF}_2$  would precipitate?
5. A solution is prepared by adding 1.5 mol  $\text{BaCrO}_4$  to water to make 1.0 L of solution. Calculate the  $[\text{Ba}^{2+}]$  and the  $[\text{CrO}_4^{2-}]$  at equilibrium.
6. The  $[\text{Ag}^+]$  of a solution is  $4.0 \times 10^{-3}$  M. Calculate the  $[\text{Cl}^-]$  that must be exceeded before  $\text{AgCl}$  can precipitate.
7. Calculate the solubility of  $\text{PbI}_2$ .
8. 30 mL of 0.10 M  $\text{AgNO}_3$  is added to 70 mL of 0.10 M  $\text{CaCl}_2$ . What is the concentration of each ion in the solution once precipitation stops and equilibrium is established?

## Solubility #6

1. Show whether or not a precipitate would be expected to form when 0.0050 g  $\text{AgNO}_3$  crystals are added to 2.00 L of 0.0010 M  $\text{NaCl}$ .
2. 2.0 mg of  $\text{Ca}(\text{NO}_3)_2$  and 2.0 mg  $\text{NaF}$  are dissolved and made up to 500 mL of solution. If the  $K_{\text{sp}}$  for  $\text{CaF}_2$  is  $4.0 \times 10^{-11}$ , will a precipitate form?
3. Will a precipitate of  $\text{AgCl}$  form when 5.1 mg of  $\text{AgNO}_3$  crystals are added to 3.0 L of  $2.0 \times 10^{-3}$  M  $\text{NaCl}$ ?
4. Show whether or not a precipitate of silver acetate forms when 15 mL of 1.0 M  $\text{AgNO}_3$  is added to 45 mL of acetic acid in which the  $[\text{CH}_3\text{COO}^-]$  is  $5.2 \times 10^{-3}$  M.  
 $K_{\text{sp}} \text{CH}_3\text{COOAg} = 3.7 \times 10^{-3}$
5. Determine whether or not a precipitate of  $\text{BaSO}_4$  will form when 0.15 g of  $\text{K}_2\text{SO}_4$  solid is added to 2.0 L of  $1.7 \times 10^{-5}$  M  $\text{BaCl}_2$ .
6. Explain why a precipitate of silver chloride will not be produced when 20 mL of  $3.0 \times 10^{-6}$  M  $\text{AgNO}_3$  is mixed with 30 mL of  $1.0 \times 10^{-4}$  M  $\text{NaCl}$ .
7. When  $\text{AgNO}_3$  crystals dissolve in a solution containing 0.010 M  $\text{NaCl}$  and 0.010 M  $\text{Na}_2\text{CrO}_4$ ,  $\text{AgCl}$  precipitates before the  $\text{Ag}_2\text{CrO}_4$ . Explain this behavior.
8. A 0.010 M solution of  $\text{AgNO}_3$  is added dropwise to a solution containing a mixture of carbonate and iodate ions, in which  $[\text{CO}_3^{2-}] = 3.0 \times 10^{-3}$  M and  $[\text{IO}_3^-] = 5.0 \times 10^{-3}$  M. Which substance precipitates first?
9. Will a precipitate of  $\text{Al}(\text{OH})_3$  form when 0.50 L of  $2.0 \times 10^{-3}$  M  $\text{AlCl}_3$  and 0.50 L of  $4.0 \times 10^{-2}$  M  $\text{NaOH}$  are mixed and diluted to 1000 L with water?  $K_{\text{sp}} \text{Al}(\text{OH})_3 = 3.7 \times 10^{-15}$
10. Will a precipitate form when 400 mL of 0.0020 M  $\text{Ba}(\text{OH})_2$  are mixed with 200 mL of 0.0020 M  $\text{H}_2\text{SO}_4$ ?



## VI. Quantitative Aspects of Solubility

Low solubility compounds form an eq<sup>m</sup> between the solid and its aqueous ions.



$$\text{Then: } K_{\text{eq}} = [\text{cation}]^n \times [\text{anion}]^m$$

If both [ion] are large, the  $K_{\text{eq}}$  is large; a large  $K_{\text{eq}}$  implies high solubility.

The  $K_{\text{eq}}$  is the product of the solubilities, so this constant is:

$$K_{\text{sp}} = \text{Solubility Product Constant}$$

### (A) Calculating the solubility

**Example 1:** Find the solubility for CuI.  $K_{\text{sp}} = 1.3 \times 10^{-12}$

**Example 2:** Find the solubility of PbCl<sub>2</sub>.  $K_{\text{sp}} = 1.2 \times 10^{-5}$

**Example 3:** Find the solubility of  $\text{Al}(\text{OH})_3$ .  $K_{sp} = 3.7 \times 10^{-15}$

**Shortcuts**

Compound	$K_{sp}$	Solubility
AB	$X^2$	$\sqrt{K_{sp}}$
$\text{A}_2\text{B}$ or $\text{AB}_2$	$4X^3$	$\sqrt[3]{K_{sp} / 4}$
$\text{A}_3\text{B}$ or $\text{AB}_3$	$27X^4$	$\sqrt[4]{K_{sp} / 27}$

**(B) Calculating the  $K_{sp}$  of a compound**

**Example 1:** A saturated solution of  $\text{PbSO}_4$  has  $[\text{Pb}^{2+}] = 1.05 \times 10^{-4}$  M. Find the  $K_{sp}$  for lead (II) sulphate.

The  $\text{Pb}^{2+}$  ion results from the dissociation of the salt. An equal number of both lead and sulphate ions would have formed. As this is a saturated sol<sup>n</sup>, the [ion] would be eq<sup>m</sup> concentrations.

**Example 2:** A saturated solution of  $\text{PbCl}_2$  has  $[\text{Pb}^{2+}] = 3.56 \times 10^{-2}$  M. Find the  $K_{\text{sp}}$  for lead (II) chloride.

For every  $\text{Pb}^{2+}$  ion there will be two  $\text{Cl}^-$  ions formed.

### (C) Concentration of other ion

**Example 1:** A solution contains  $[\text{Pb}^{2+}] = 1.0 \times 10^{-3}$  M. If the  $K_{\text{sp}}$  for  $\text{PbSO}_4$  is  $1.8 \times 10^{-8}$ , what is the maximum possible  $[\text{SO}_4^{2-}]$ ?

This is not a case of forming ions by dissociation of the salt, but rather mixing two solutions together. In this case, the [ions] must meet the  $K_{\text{sp}}$  value.

**Example 2:** A solution contains  $[\text{Pb}^{2+}] = 2.0 \times 10^{-3}$  M. If the  $K_{\text{sp}}$  for  $\text{PbCl}_2$  is  $1.2 \times 10^{-5}$ , what is the maximum possible  $[\text{Cl}^-]$ ?

